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Atmospheric density, pressure and temperature profile reconstruction from refractive angle measurements in stellar occultation

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Introduction

- We have studied possibility of atmospheric density, pressure and temperature reconstruction from refractive angle measurements in stellar occultation
- Stellar occultation instruments have high pointing accuracy and they follow point-like sources \Rightarrow direct accurate measurements of the refractive angle
- Part of ESA project SARFOI ; FMI-SSF-ESA-TERMA
- Goals:
 - Development of model and inversion algorithm
 - Assessment of possible error sources and sensitivity of the retrieval to them
 - To derive pointing accuracy requirements for temperature profiling with accuracy 1–2 K and vertical resolution 1–2 km (for COALA instrument)
 - Analyze the accuracy attainable in temperature profiling with GOMOS instrument



Stellar occultation measurements

- Altitude range 120–10 km
- Reference point at the altitude ~ 120 km
- Pointing system: scanning mirror + star tracker
- Sampling frequency of refractive angle measurements ~ 100 Hz
- Wavelength range photometers
 - *GOMOS* 625–950 nm
 - *COALA* 675–775 nm
- Instrumental noise
 - *Random component*
 - *Harmonic component*

	<i>GOMOS</i>	<i>COALA</i>
Instrumental noise at 2 Hz	2.75 μ rad	1–2 μ rad
Signal–to–noise ratio at 40 km	16.7	23–46



Forward model

density profile \Rightarrow *refractive angle*

Assumptions:

- Dependence of the refractive index on the wavelength (Edlen formula)

$$n = 1 + C(\lambda) \frac{\rho}{\rho_0}$$

- Spherical symmetry assumption

Refractive angle

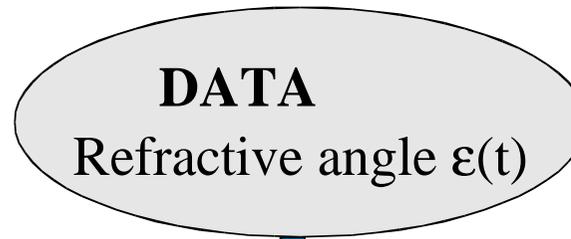
$$\varepsilon = -2 \int_{r_t}^{\infty} \frac{d(\ln n)}{dr} \frac{a dr}{\sqrt{n^2 r^2 - a^2}}$$

Error of forward model

< 0.1 K in temperature reconstruction



Inversion



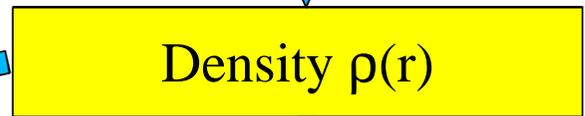
Inverse Abel transform

$$\epsilon(a) = -\int_a^{\infty} \frac{2a \ln(n(z))' dz}{\sqrt{z^2 - a^2}}$$



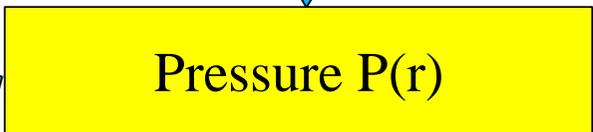
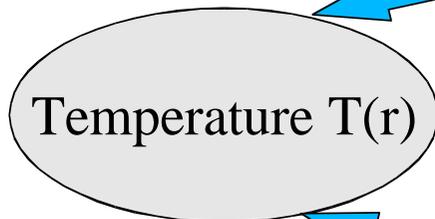
Edlen formula

$$\rho(r) = \frac{\rho_0}{C(\lambda)} (n(r) - 1)$$



Hydrostatic equation

$$P(r) = \int_r^{\infty} g(x) \rho(x) dx$$



State equation of ideal gas

$$T(r) = k \frac{P(r)}{\rho(r)}$$



Error analysis

- Error analysis: Monte–Carlo simulation
- Instrumental noise : additive Gaussian noise
- Inversion statistics:
 - *rms error (from true value)*
 - *bias*



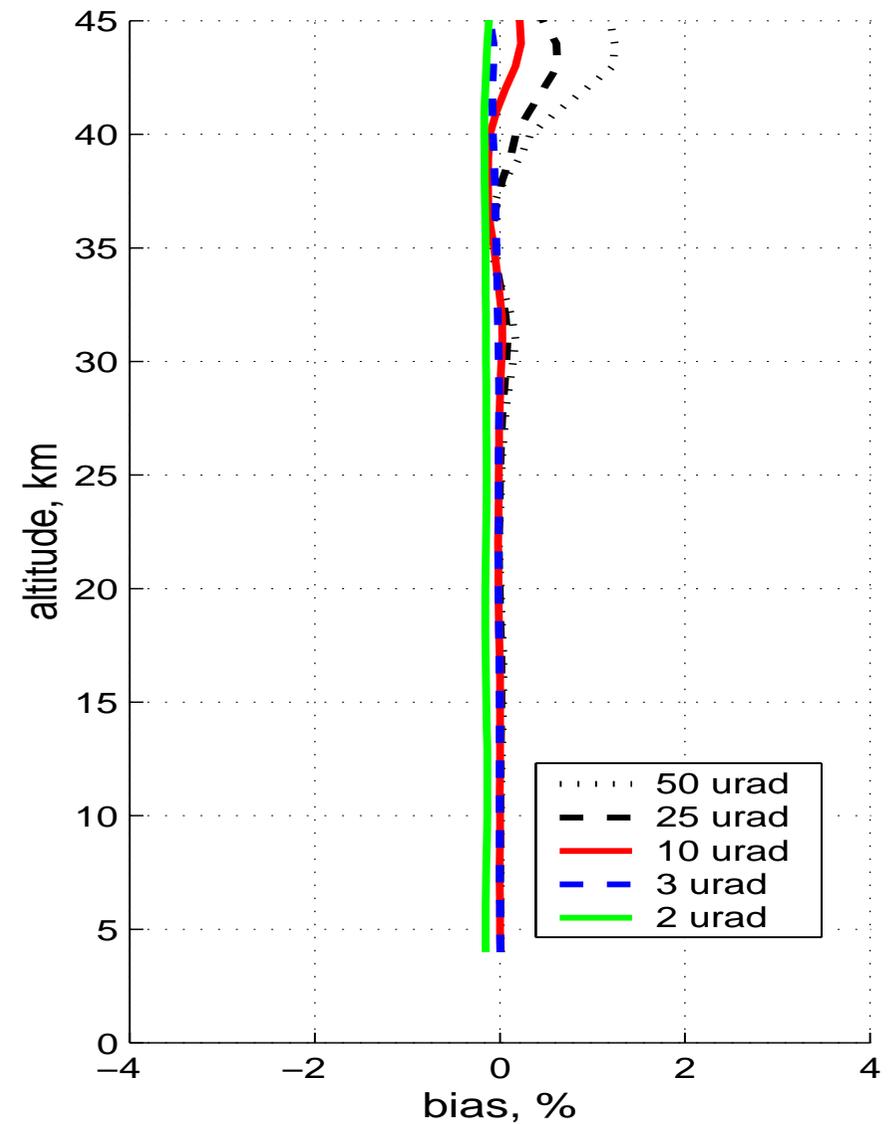
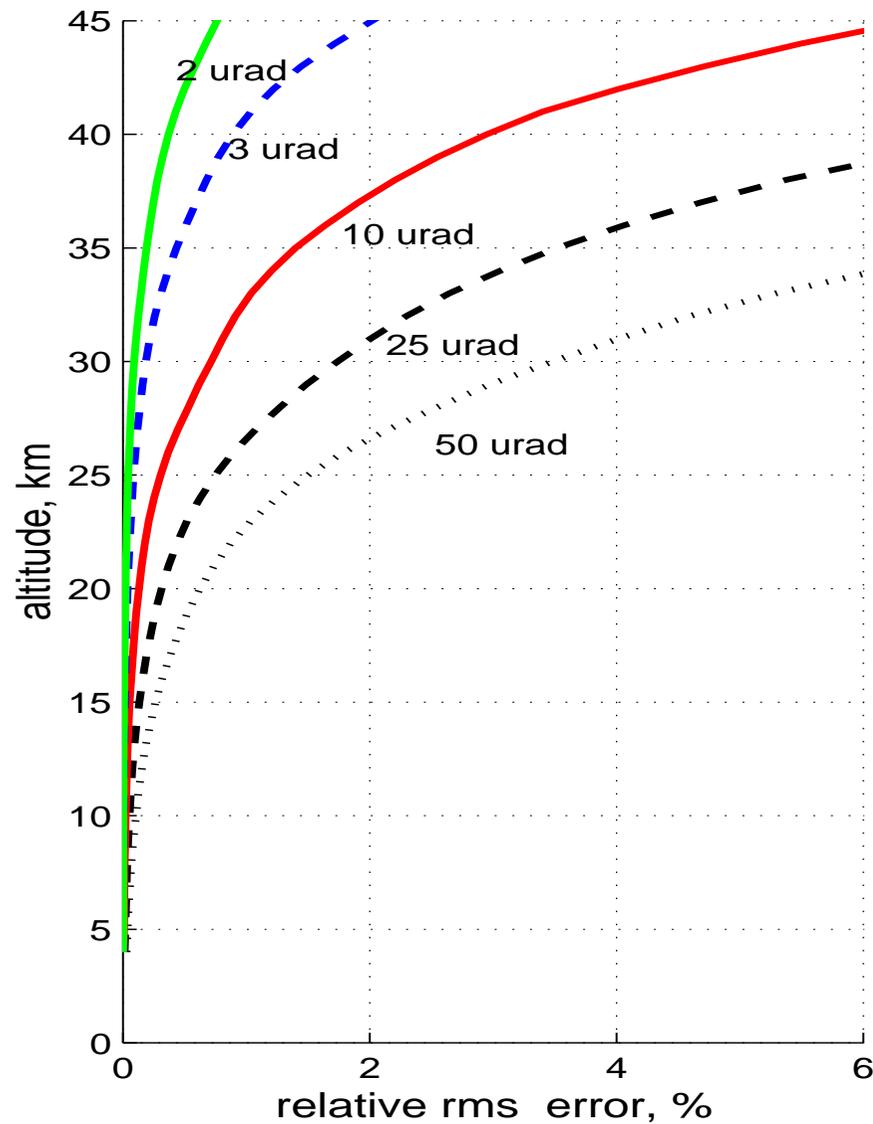
Error sources

- Instrumental error
- Sampling frequency of measurements
 - *vertical resolution*
 - *accuracy of retrieval*
- Chromatic smoothing < 0.01 K
- Scintillation effect < 0.1 K



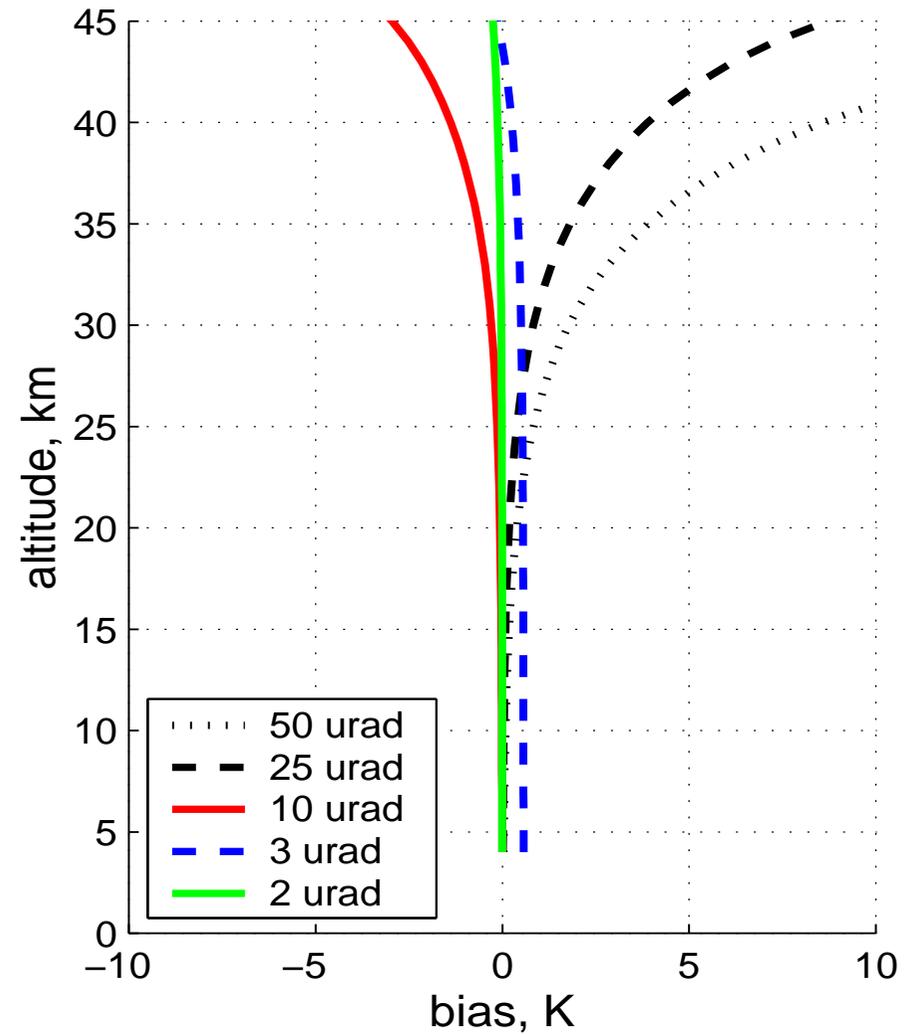
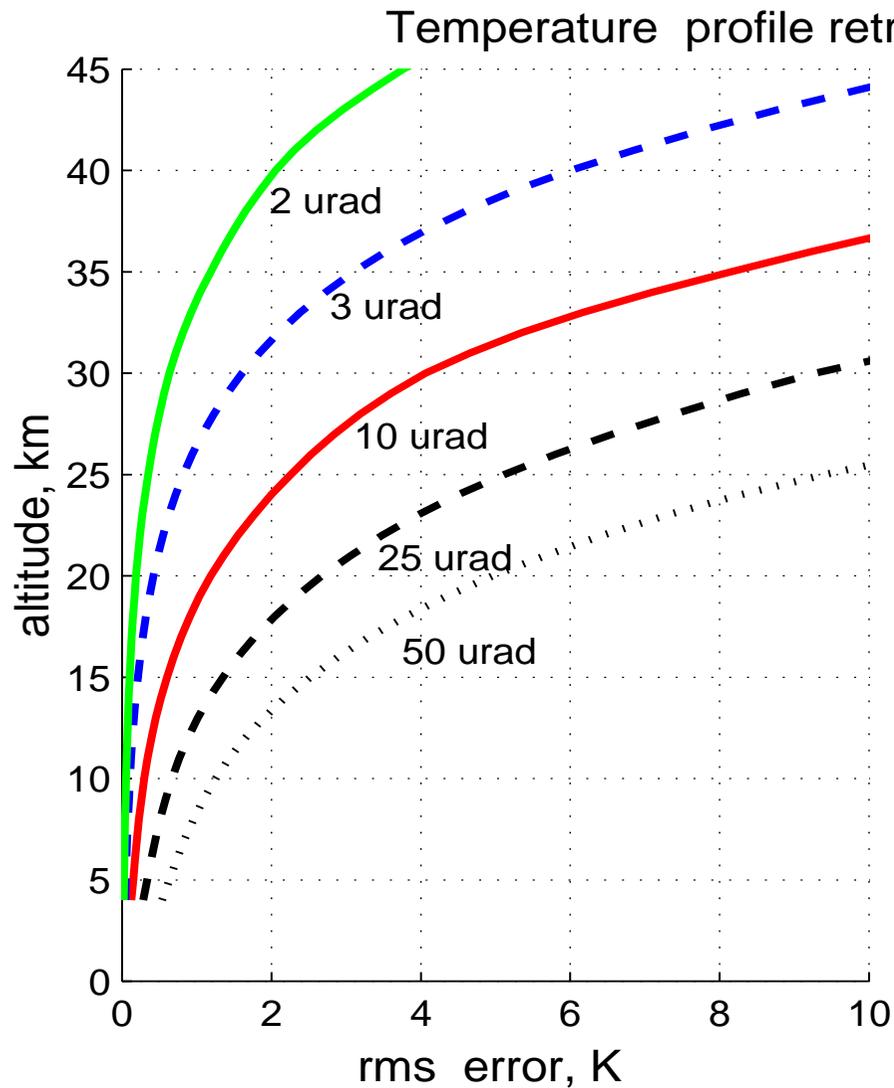
Instrumental error. Density profile retrieval

Density profile retrieval. Abel inversion. Additive noise





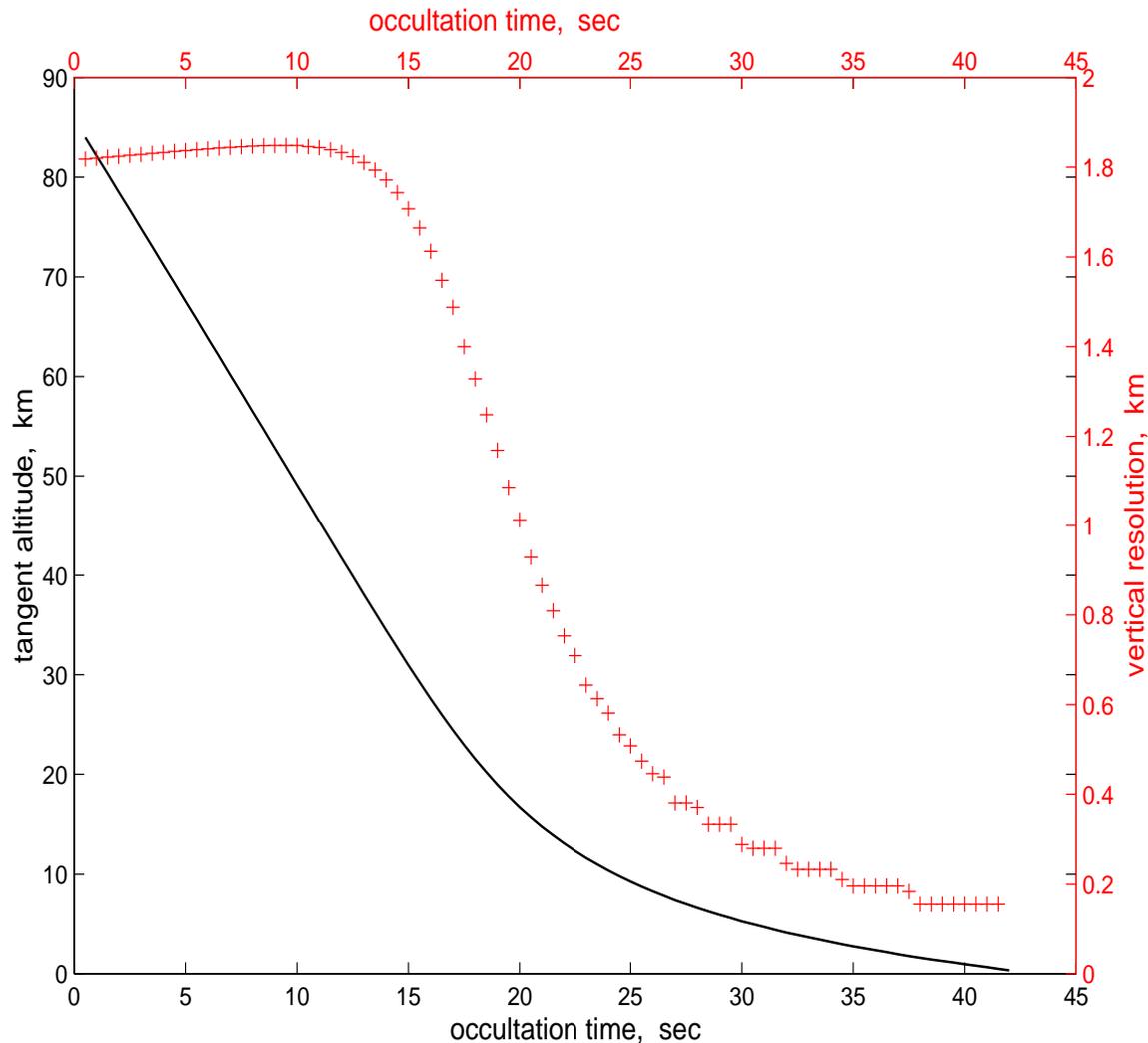
Instrumental error. Temperature profile retrieval





Sampling frequency of measurements.

Vertical resolution



<i>Sampling frequency</i>	<i>Vertical sampling resolution</i>	
	<i>High altitudes</i>	<i>Mean</i>
200 Hz	18.4 m	11.4 m
100 Hz	37 m	23 m
50 Hz	74 m	46 m
20 Hz	185 m	114 m
10 Hz	369 m	228 m
2 Hz (0.5s)	1.8 km	1.14 km



The effect of smoothing before inversion

Considered cases

- 21 μ rad at 100 Hz
- 3 μ rad at 2 Hz
- 3 μ rad at 100 Hz

Questions

- An advantage of smoothing prior to the inversion (compare cases

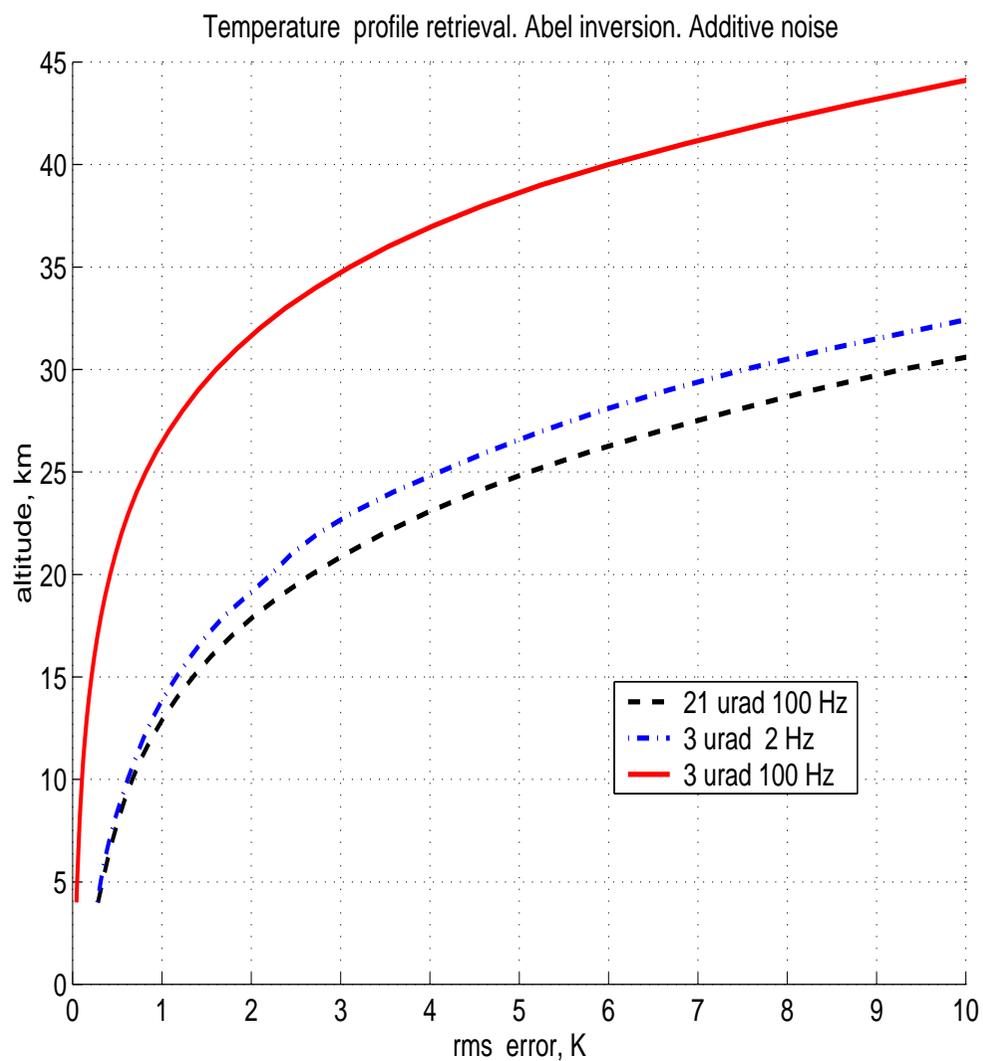
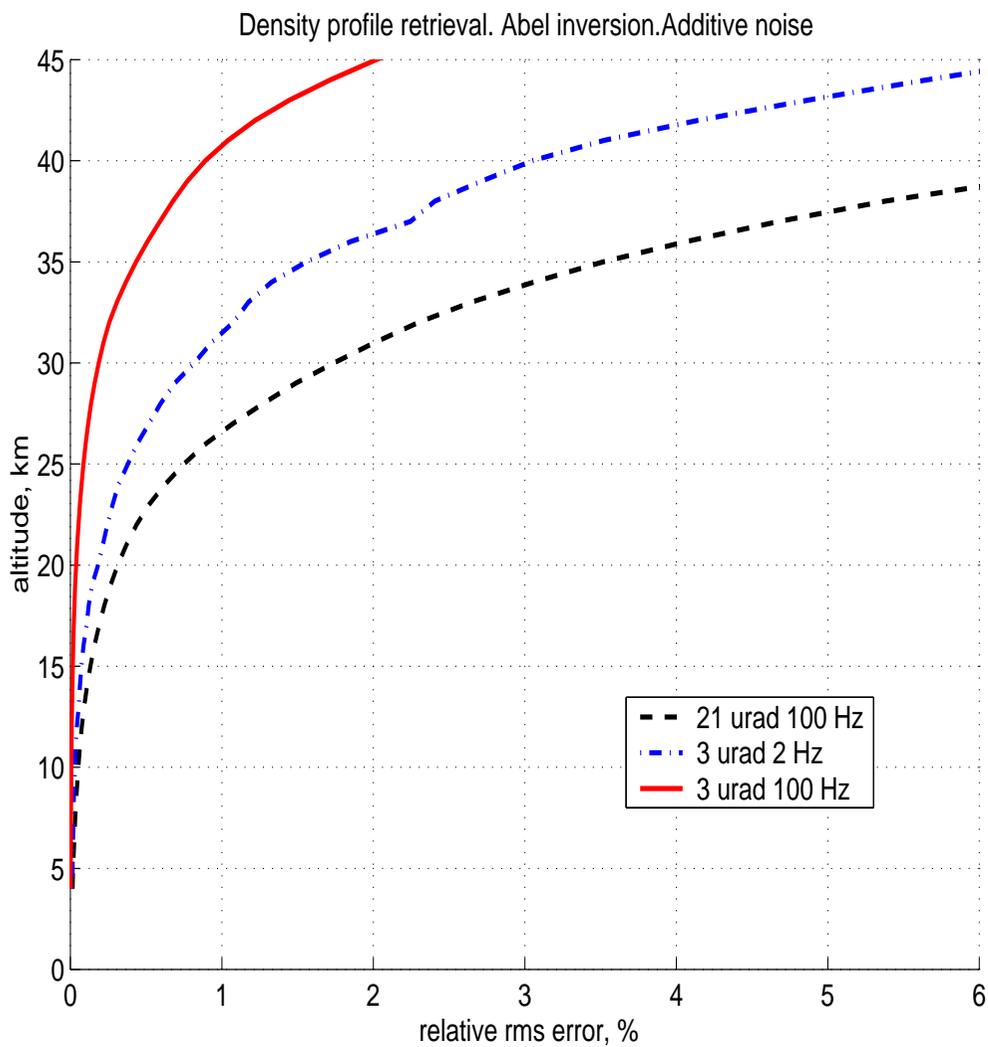
21 μ rad @ 100Hz and 3 μ rad@2 Hz)

- Smoothing properties of the inversion procedure

(cases 3 μ rad @2 Hz and 3 μ rad @ 100 Hz)



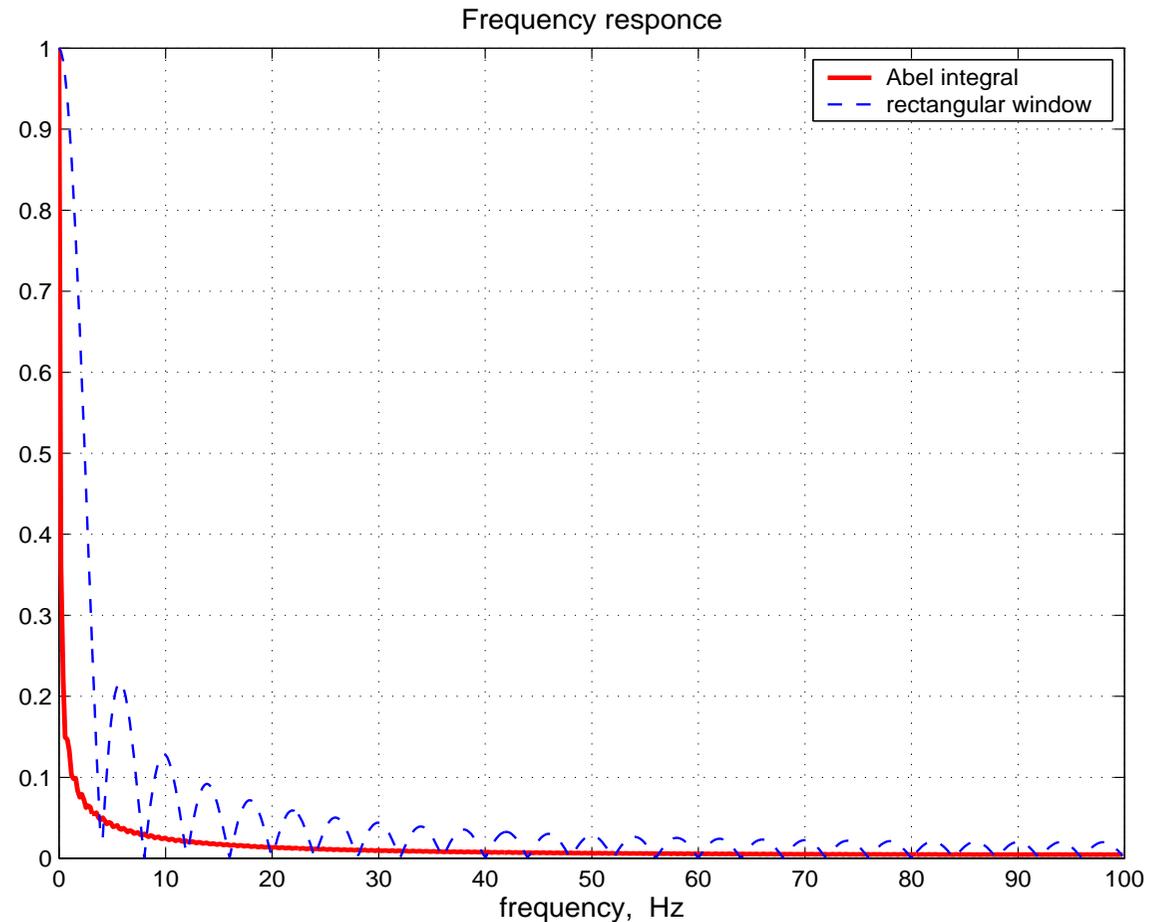
The effect of smoothing prior to inversion





Smoothing properties of inversion

- Temperature reconstruction contains two smoothing procedures
 - *Abel inversion*
 - *integration in the pressure reconstruction*

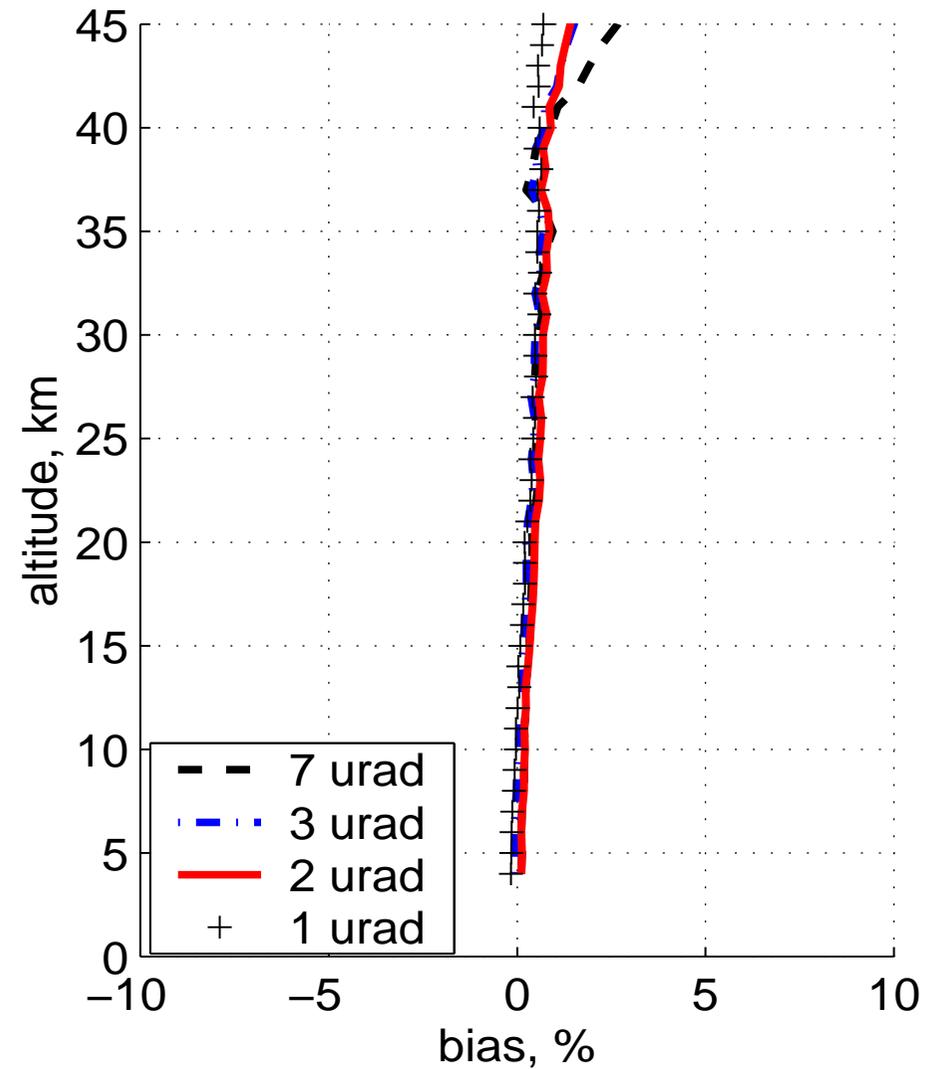
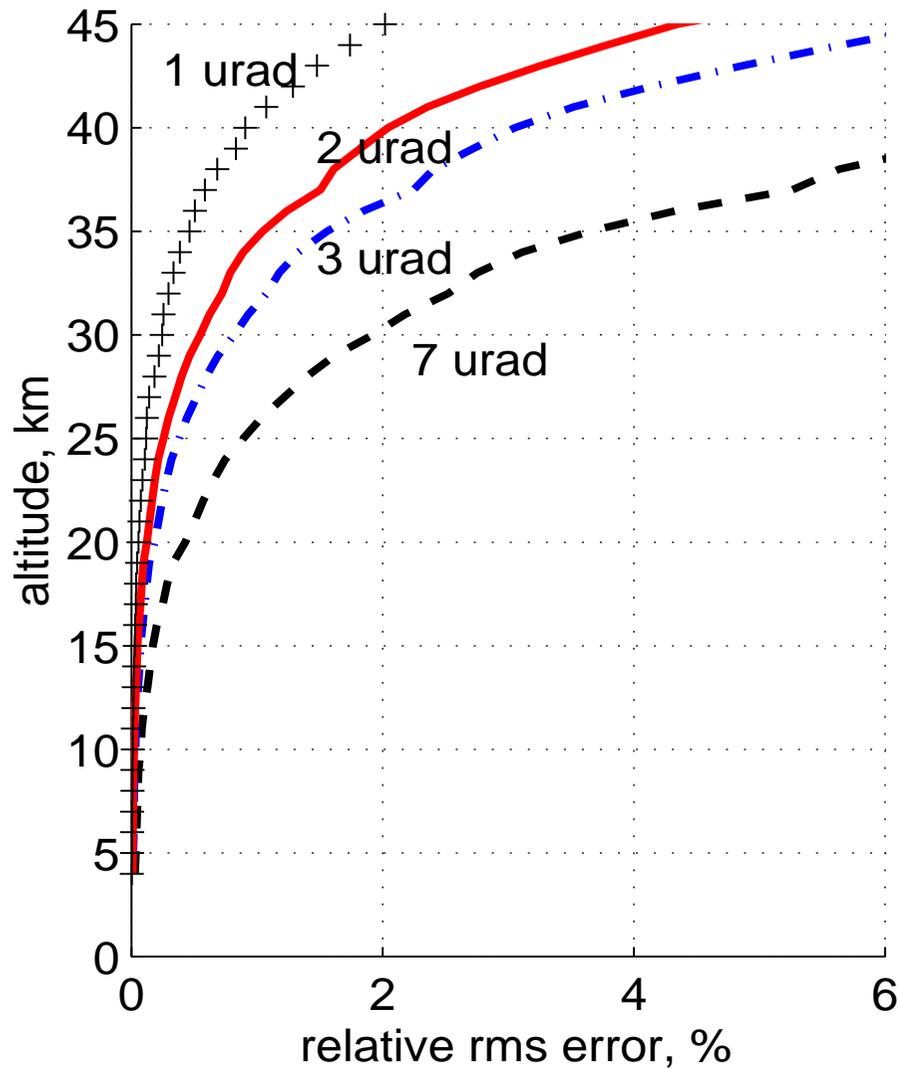


Frequency response of Abel integral



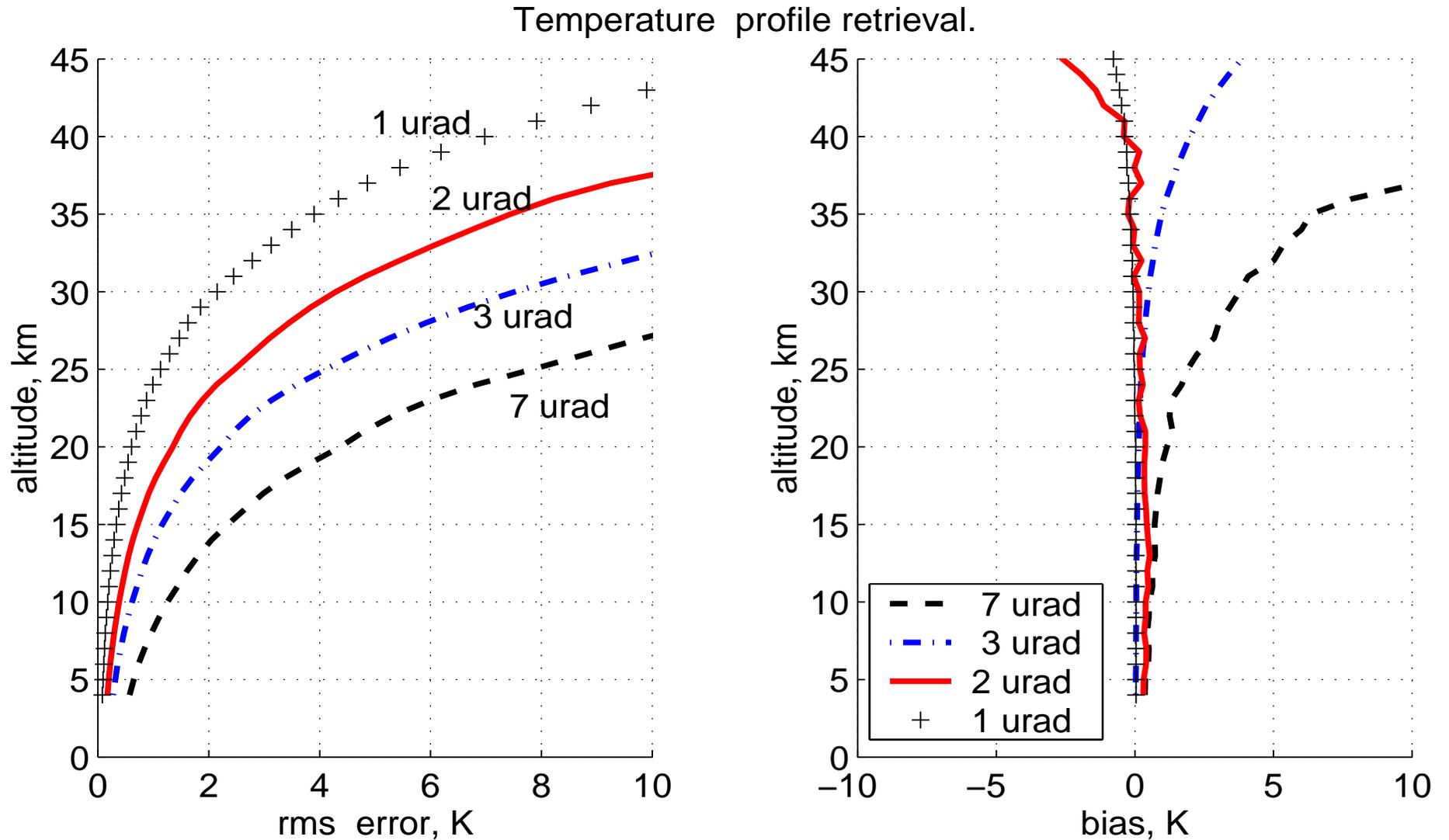
Accuracy of density retrieval at 2 Hz sampling frequency

Density profile retrieval.





Accuracy of temperature retrieval at 2 Hz sampling frequency





Summary

- The main source of error in temperature and density retrieval is the non-accurate measurements of the refractive angle.
- Both instrument noise level and sampling frequency of measurements are very important for retrieval.
- In order to obtain the temperature profile with accuracy of 1–2 K and vertical resolution 1–2 km for altitudes up to 35–40 km the refractive angle should be measured with accuracy better than 1 μ rad at 2 Hz sampling frequency
- Reality for stellar occultation : temperature profiling with accuracy 2 K up to
 - GOMOS: 22 km
 - COALA: 30 km